

Today's Exercise: security and privacy and building an encryption module!

- First understand the problem and design a solution
- Next implement an “application” in Python
 - Application: You want your photograph(s) to be viewable only by authorized people

Security & Privacy Exercise: Encryption

- Encryption – coding your messages
 - Sending secrets
 - Safeguard your private information!
- Caesar's Cipher – a simple 'substitution cipher' algorithm
 - History: used by Julius Caesar to send military secrets
- Original Form: Shift each alphabet by 3
 - A replaced by D, B replaced by E,Y replaced by B
 - Circular shift
 - "FRIDAY" encrypted as " IULGDB "

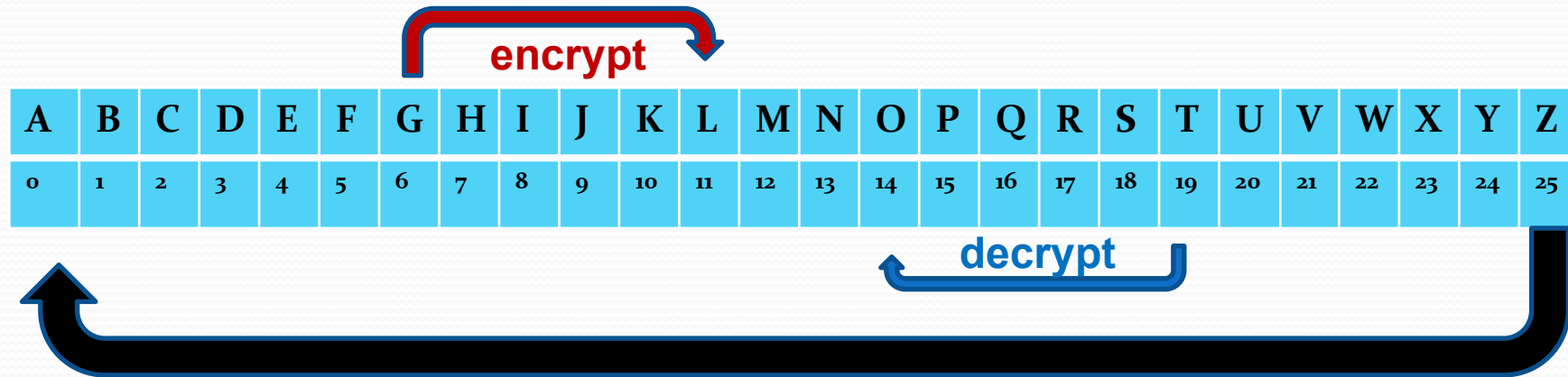
Generalized Shift(Caeser) Cipher.

- Instead of shifting by 3, shifted by some secret value K
 - K is between 0 and 25
 - Why ? Because there are 26 letters in the alphabet
- The value K is your secret “Key” (like a password)
- Encryption “algorithm” : Shift each letter by K
- To “decrypt” the message: Shift ‘left’ each letter by K
- Some math: we can assign a number from 0 to 25 to each letter in the alphabet starting with A
 - Shifting by K means adding K to that number
 - But circular addition...more in a bit

Example:

Message: **GOODBYE**
Key: $K = 5$

Encrypted message:
LTTIGDJ
(G replaced by L, O by T, ...)



To decrypt the encrypted message, move letter left 5 places

So what's the "math" behind this..

- Algorithms need to be shown to be "correct"
- This is where the math comes in !

Some Math...the CS "discrete" math:

Circular Addition uses Modulo arithmetic:

$(A+K) \bmod N = \text{remainder of } (A+K) \text{ divided by } N$

Ex: $(6+5) \bmod 26 = 11$ (*letter L*),

$(24+5) \bmod 26 = 3$ (*which is letter D*)

To decrypt: $(B - K) \bmod N$

If $(B-K)$ is negative it adds N to get result.

$(3 - 5) \bmod 26 = -2 + 26 = 24 = \text{letter Y}$

Modulo arithmetic in Python

- Circular addition
 - Circular addition.....known as Modulo
 - $A \text{ Mod } N = \text{remainder of } A \text{ divided by } N$
- Good news: Python provides the Modulo operation
 - **$B = a \% N$**
- To encrypt value a with key K : $B = (a+K) \text{ mod } N$
 - For alphabet $N=26$ (we have 26 different values)

Weak encryption vs Strong encryption

- Strength of encryption = How easy is it to decipher your secret (i.e., encryption)
- In Caesar's cipher we use the same key for each character in our message
 - Shift each alphabet by 5
- Another method: version of One-Time-Pad (OTP)
- Encrypt each position in message with a separate key
 - Message = BYE
 - Shift B by 3, shift Y by 7, shift E by 5 to get EFJ

Your first exercise...in breakout groups

- Encryption 1 using Caesar's cipher (circular shift):
 - Each of you chooses a key
 - Each chooses a day of the week (Monday through Sunday) and encrypts the day.
 - ONE of you shares your encrypted message (day of the week)
 - Can others in the group guess the message ?
- Encryption 2: using One time pad
 - Choose one of these words: Monday, Sunday, Friday
 - One of you encrypts the word they chose using one-time pad (a unique key for each position in the 6 letter word)
 - Share your encrypted message
 - Can the others guess (in one guess) what exactly the word is ?

A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25



An application using Encryption & implementation in Python today....

- You want to send a picture (your selfie) to a friend
 - Or better yet, post it on a website
- To restrict who can see it, you want to encrypt it and only those with the correct key will be able to see the picture
- Steps:
 1. Take your selfie
 2. Import into your Python code and enter a secret Key
 3. Write (and run) python code to encrypt the selfie
 - Implement the encryption algorithm we discussed
 4. Decrypt with the key – a wrong key will lead to a jumbled image
- Checking your encryption: Look at the encrypted image and see how similar it looks to the original image
 - The less similar it looks the “better” the encryption!

Getting Started...some preliminaries

- An image (i.e., your selfie) is a matrix of pixels
- To simplify our algorithm (for purpose of demonstration!) we convert your image to a grayscale image
- input image is a N by M matrix $A[i,j]$ of pixels and key= K
 - Each pixel $A[i,j]$ has a greyscale value between 0 and 255
 - i.e., 256 different values – analogy with 26 letters in alphabet
- To encrypt image, for each pixel add K to $A[i,j]$ to get $B[i,j]$
 - Important: Circular addition with 256 different values
 - Python operator: %
 - $B[i,j] = (A[i,j] + K) \% 256$

A better encryption "system"

- We saw how the one-time pad (OTP) is a better technique
- Applying the concept to this system: each pixel $A[i,j]$ has its own key $K[i,j]$
 - And then algorithm is $B[i,j] = (A[i,j] + K[i,j]) \% 256$
- Here is a cool trick: instead of entering gazilion values of $K[i,j]$, how about using a 'secret' image as your key ?!!
 - Key image K , represented as a matrix $K[i,j]$
- Change to algorithm:
 - import the key image as $K[i,j]$ convert to greyscale
 - $B[i,j] = (A[i,j] + K[i,j]) \% 256$